

1.) Erin and Christa were working on cubing binomials for math homework. Erin believed they could save time with a shortcut. She wrote down the rule below for Christa to follow.

$$(a+b)^3 = a^3 + b^3$$

Does Erin's shortcut always work? Justify your result **algebraically**.

$$(a+b)(a+b)(a+b)$$

$$(a+b)(a^2+ab+ab+b^2)$$

$$(a+b)(a^2+2ab+b^2)$$

$$a^3 + 2a^2b + ab^2 + a^2b + 2ab^2 + b^3$$

**NO**

$$a^3 + 3a^2b + 3ab^2 + b^3 \neq a^3 + b^3$$

2.) Algebraically prove that  $\frac{x^3+9}{x^3+8} = 1 + \frac{1}{x^3+8}$

$$\frac{x^3+9}{x^3+8} = \frac{1}{1} + \frac{1}{x^3+8}$$

$$\frac{x^3+9}{x^3+8} = \frac{x^3+8}{x^3+8} + \frac{1}{x^3+8}$$

$$\frac{x^3+9}{x^3+8} = \frac{x^3+9}{x^3+8} \quad \checkmark$$

3.) Algebraically prove that:  $x^3 - 2x^2 - 4x + 8 = (x+2)(x-2)^2$

$$x^3(x-2) - 4(x-2) = (x+2)(x-2)^2$$

$$(x-2)(x^2 - 4) = (x+2)(x-2)^2$$

$$(x-2)(x-2)(x+2) = (x+2)(x-2)^2$$

$$(x-2)^2(x+2) = (x+2)(x-2)^2 \quad \checkmark$$

4.) Verify the following Pythagorean identity for all values of  $x$  and  $y$ :

$$(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$$

$$(x^2 + y^2)^2 = (x^2 - y^2)(x^2 - y^2) + 4x^2y^2$$

$$(x^2 + y^2)^2 = x^4 - x^2y^2 - x^2y^2 + y^4 + 4x^2y^2$$

$$(x^2 + y^2)^2 = x^4 + 2x^2y^2 + y^4$$

$$(x^2 + y^2)^2 = (x^2 + y^2)(x^2 + y^2)$$

$$(x^2 + y^2)^2 = (x^2 + y^2)^2 \quad \checkmark$$